ECERFACS





EUROPEAN CENTRE FOR RESEARCH AND ADVANCED TRAINING IN SCIENTIFIC COMPUTING

Tools for the numerical simulation with complex chemistry **Open-source code CANTERA**

Tuesday 16th November 2020

Jonathan WIRTZ, Théo OGIER - PhD CERFACS

www.cerfacs.fr



- 9h30 10h30 : Talk about Cantera (J.W)
- 10h30 12h30: jupyter notebook tutorial (J.W + T.O)
- 12h30 14h: Lunch break (yourself:D)
- 14h 14h15: Talk about cantera-avbp features (J.W)
- 14h15 17h: end of jupyter notebook tutorial + create your own script (J.W + T.O)

Everything will be on teams.



Why studying chemistry at CERFACS ?

Pollutants



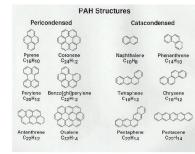
<u>Chemistry driven processes</u>

Ignition



Fuel addition







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Content of the presentation

- I. Presentation of CANTERA
- II. Governing equations and numerical methods III. Practical use
- IV. Installation

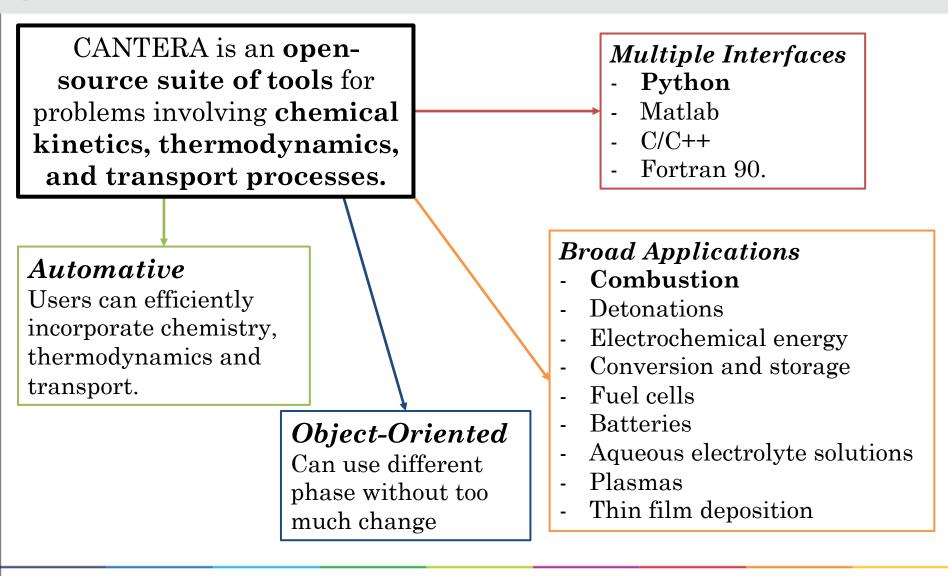


Content of the presentation

I. Presentation of CANTERA

- 1) What is CANTERA ?
- 2) What can it do ?
- 3) Why is it a good choice ?
- 4) How will it be helpful to you ?



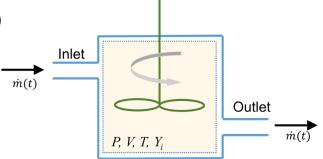


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In terms of calculations ...

- Initialize a mixture (tutorial part 1)
- ◆ 0D (tutorial part 2)
 - Equilibrium state
- ◆ 0D with time evolution (tutorial part 3)
 - Constant Pressure/Volume batch reactor
 - Steady-state Plug Flow Reactor (PFR)



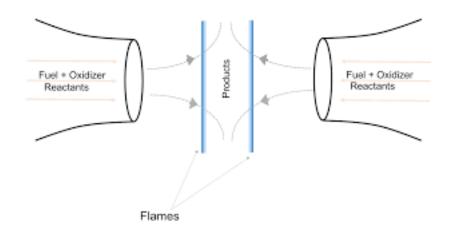




What can CANTERA do?

◆ 1D (tutorial part 4)

- Burner stabilized and propagating premixed flat flame
- Diffusion flame in counterflow configuration
- Premixed flame in counterflow configuration (strained)





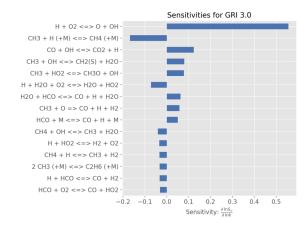


What can CANTERA do?

... but also in terms of analysis !

◆ Data extraction and post processing:

- Temperature, Pressure, Mass Fractions ...
- Path Flow analysis, sensitivity analysis
- \blacklozenge Add surface chemistry and heat losses ...



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CANTERA's history

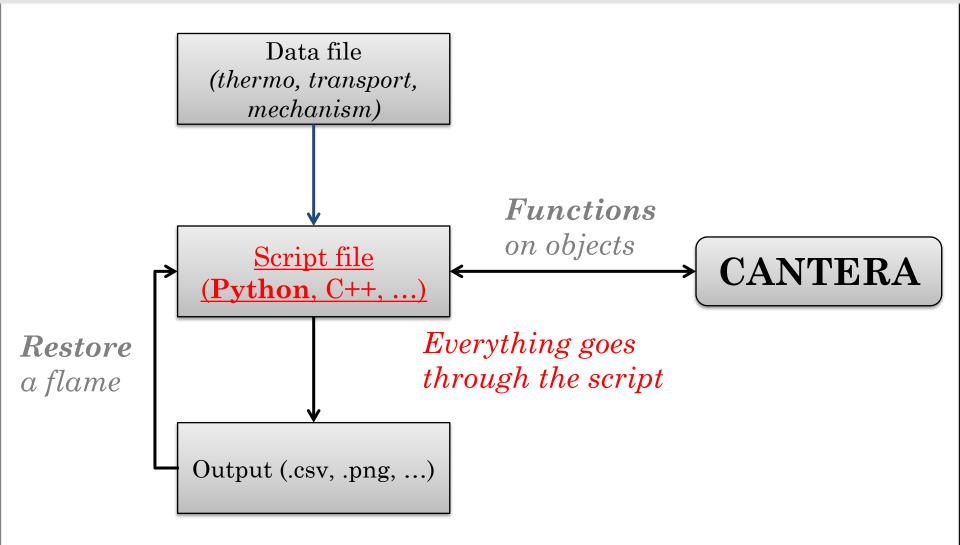
- We owe it all to <u>Dave Goodwin</u>, the original developer of Cantera whom made it available under BSD license.
- He started off with an extensive overhaul of the CHEMKIN suite ...
- ... to steer the modeling software towards an objectoriented structure with multiple interfaces (C++, Python, Matlab, FORTRAN).
- Currently, we are at the version 2.4.0 (but we will use version 2.3 in this training).



CANTERA has the advantages of an objectoriented code (info in <u>appendix</u>):

- Think of a Lego box : it allows you to form complex kinetic/thermodynamic systems, or networks from a set of « building blocks ».
- Each « building block » (or object) represents a welldefined small component of the global structure.
- Those « building blocks » are defined and coded in C++, the core language of CANTERA ...
- ... But CANTERA provides a user-friendly interface in Python (or Matlab, or FORTRAN)





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- CANTERA has most of the functionality of the familiar CHEMKIN-II + additional capabilities (non-ideal phases, multiphase equilibrium, electrochemistry...) See <u>appendix</u> to know more the difference between CANTERA and CHEMKIN.
- CANTERA can (re)use CHEMKIN files (libraries, mechanisms ...).
- Users can interface with Cantera through Python, C++, the Matlab toolbox and Fortran as well : no language excuse !
- Those interfaces are only front ends; calculations are done in an optimized, compiled code that is really efficient and fast.
- Basically, it is possible to create anything that pops into your head ...





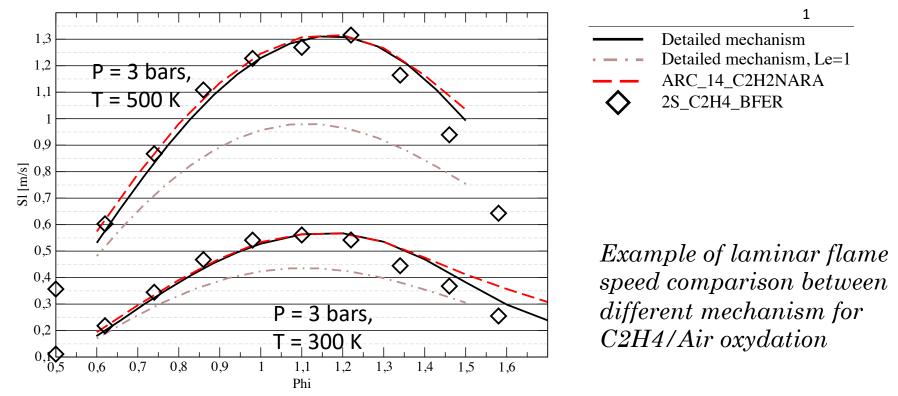
- * On the downside : CANTERA does not provide any robust documentation. Basically, everything that exists can be accessed through : http://www.cantera.org
- **But** there is a big community of users, they will help solve all bugs and scripting issues : cantera google group
- CANTERA comes with a series of scripts and examples in all of the interface languages : currently in the folder 'samples'



How will it be helpful to you ?

1. Validation phase

✓ Compare different chemistries with CANTERA, including skeletal and reduced chemistries, in a fast and efficient way.



¹ K. Narayanaswamy, G. Blanquart, H. Pitsch "A consistent chemical mechanism for oxidation of substituted aromatic species ". Combustion and Flame, Vol.157 pp. 1879–1898, 2010



How will it be helpful to you ?

1. Validation phase

Simulate chemistry-related combustion features directly

- **Evaluate the impact of simplified transport model** (constant Schmidt number, fitted viscosity ...)
- **Develop and test various combustion models**. At CERFACS, we use a flame front thickening option (DTFLES) in our CFD code AVBP
- Evaluate the effects of strain on flame behavior: axisymmetric stagnation flows reduce to pseudo 1D simulations (counterflow flames)





How will it be helpful to you ?

- 1. Validation phase
- 2. Reduce some chemistries
- Reduce chemistries
 - Implement your own via the main script (Sensitivity Analysis, ...)
 - Extract relevant data for post processing with reduction tools (ARCANE)



- 1. Validation phase
- 2. Reduce some chemistries
- 3. Initialization phase for other codes
- Use 1D profiles to initialize a simulation (CFD codes such as AVBP at CERFACS)
- Use 1D profiles to generate flamelet tables for use in CFD codes (Mutagen at CORIA)





Content of the presentation

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- II. Governing equations and numerical methods
- III. Practical use
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Content of the presentation

II. Governing equations and numerical methods

- 1) (0D) Equilibrium equations
- 2) (0D in time) Usual reactors equations
- 3) (1D) Laminar premixed flame equations





Equilibrium calculations

"The equilibrium state is that corresponding to **a minimum of a property** called the energy function under specified conditions"

Cantera related pages : <u>https://cantera.org/tutorials/python-tutorial.html / https://cantera.org/tutorials/cxx-guide/equil-example.html</u>





"The equilibrium state is that corresponding to a minimum of a property called the energy function under specified conditions"

- Several methods exist, based on different energy functions.
- Usually, the Gibbs free energy function is used, with two constant quantities
- ◆ 2 different methods exist :
 - Non-stoichiometric methods where the conservation of mass is treated separately
 - **Stoichiometric methods**, more robust but slower

CANTERA tries a non-stoichiometric method first, and turns to a stoichiometric method (VCS algorithm²) if it fails.

¹ C.H.Wong ,"Chemical equilibrium analysis of combustion proudcts at constant volume", 2001
 ² Smith, W.R. and Missen, R.W. "Chemical Reaction Equilibrium Analysis: Theory and Algorithms", 1982

Governing equations Equilibrium equations

The non-stoichiometric method

Once the λ_l are determined, since **T & P are constant**, the mole fractions are automatically deduced.

$$\mu_k = \sum_{l=1}^L \lambda_l n_{kl} \Longrightarrow X_k = \frac{P_o}{P} \exp(-\frac{g_k^0(T)}{RT} + \sum_{l=1}^L n_{kl} \frac{\lambda_l}{RT})$$

- > General procedure (see <u>appendix</u> for details) :
- The g_k^0 are tabulated.
- The user provides a guess for enough $(L)X_k$ with the knowledge that $\sum_{k=1}^{L} X_k = 1$
- The chemical potential of the elemental species per atom λ_l are calculated (see appendix).
- The unknown X_k are calculated with those estimated λ_l and $\sum_{k=1}^{L} X_k = 1$ is evaluated.
- If $\sum_{k=1}^{L} X_k = 1$ is « too far » from 1, a new guess for the X_k is provided and the procedure reiterates with well chosen (L) X_k .

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Governing equations Equilibrium equations

(Note: no need to provide reactions information !)

Adiabatic flame temperature

Equilibrium calculation are also possible maintaining other quantities constant Ex: **H and P constant, through a loop on T**

$$X_{k} = \frac{P_{o}}{P} \exp\left(-\frac{g_{k}^{0}(T)}{RT} + \sum_{l=1}^{L} n_{kl} \frac{\lambda_{l}}{RT}\right)$$

and
$$\Delta H = 0$$

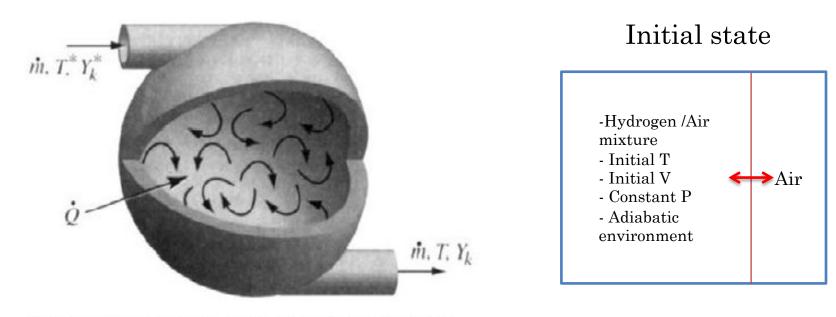
Using H at initial conditions

$$H = \int_{T_0}^T C_p dT + \sum_{k=1}^K X_k H_{f,k}^{0,m}, \quad C_p = \sum_{k=1}^K X_k C_{p,k}^m$$

 \rightarrow Gives the **gas composition** and the **adiabatic flame temperature**.



Batch and Stirred Reactor equations³



Conceptual illustration of a continuously stirred tank reactor.

³ Picture from Robert J. Kee, Michael E. Coltrin and Peter Glarborg, "Chemically Reacting Flow: Theory and Practice", 2003 – chap 16 Cantera related page : <u>https://cantera.org/science/reactors.html</u>

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The **state variables** for Cantera's general reactor model are

- \bullet *m*, the mass of the reactor's contents
- V, the reactor's volume
- ${\scriptstyle \bullet}$ $U\!,$ the total internal energy of the reactors contents
- Yk , the mass fractions for each species
- Reactor Volume:

$$\frac{dV}{dt} = \sum_{w} f_{w} A_{w} v_{w}(t)$$

Where :

- A_w is the wall Area
- $v_w(t)$ is the velocity of the wall
- $f_w = \pm 1$ is the wall facing

Mass Conservation:
$$\frac{dm}{dt} = \sum_{in} \dot{m}_{in} - \sum_{out} \dot{m}_{out} + \dot{m}_{wall}$$

Where $m_{in,out}$ are inlets and outlets mass flow rate and m_{wall} stands for the production of homogeneous phase species on the reactor walls.

³ Robert J. Kee, Michael E. Coltrin and Peter Glarborg ,"Chemically Reacting Flow: Theory and Practice", 2003 – chap 16
 ⁴ http://cantera.github.io/docs/sphinx/html/reactors.html



The state variables for Cantera's general reactor model are

- \bullet *m*, the mass of the reactor's contents
- V, the reactor's volume
- \bullet U, the total internal energy of the reactors contents
- Yk, the mass fractions for each species
- Species conservation:

$$\frac{d(mY_k)}{dt} = \sum_{in} \dot{m}_{in} Y_{k,in} - \sum_{out} \dot{m}_{out} Y_k + \dot{m}_{k,gen}$$

Where

 $m_{k,gen}$ is the rate at which species k is generated through homogeneous phase reactions in the reactor and on the walls

Energy Conservation (*reactor case*) :

$$\frac{dU}{dt} = -p\frac{dV}{dt} - \dot{Q} + \sum_{in} \dot{m}_{in} h_{in} - h\sum_{out} \dot{m}_{out}$$

Where Q is the total rate of heat transfer through all walls

³ Robert J. Kee, Michael E. Coltrin and Peter Glarborg ,"Chemically Reacting Flow: Theory and Practice", 2003 – chap 16
 ⁴ http://cantera.github.io/docs/sphinx/html/reactors.html

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Resulting system of Ordinary Differential Equations (ODE) :

- Usually stiff
- Integrated for a user-specified timestep by the Sundials' solver CVODE.

→ Gives the temporal evolution of the quantities inside a vessel

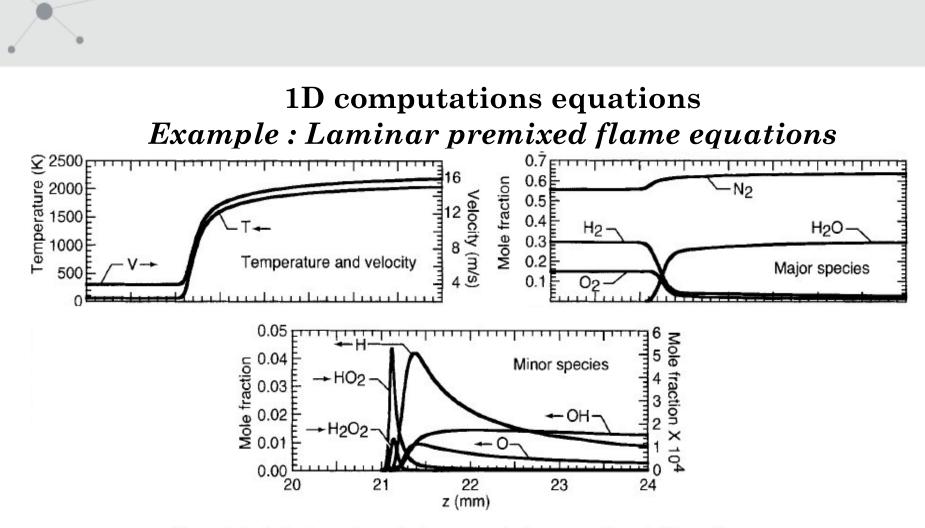
³ Robert J. Kee, Michael E. Coltrin and Peter Glarborg , "Chemically Reacting Flow: Theory and Practice", 2003 – chap 16
 ⁴ http://cantera.github.io/docs/sphinx/html/reactors.html



The constant pressure batch reactor Initial state Time evolution of the state with CANTERA 3000 0.016 2800 0.014 2600 0.012 S -Hydrogen /Air 2400 Fa 0.010 Ignition mixture i R 2200 0.008 - Initial T timing 2000 - Initial V Air 1800 0.004 - Constant P 1600 0.002 - Adiabatic 1400 0.000 0.0005 0.0010 0.0020 0.0025 0.0005 0.0010 0.0015 0.0015 0.0020 0.0025 environment Time (s) Time (s) 0.0007 0.0020 0.0006 0.0015 0.0005 Mass Fraction Separating moveable wall, to keep a constant P 0.0004 0.0003 Ŷ 0.0002 0.0005 A « piston-like » system 0.0001 0.0000 0.0025 0.0000 0.0005 0.0010 0.0015 0.0020 0.0005 0.0010 0.0015 0.0020 0.0025 Time (s) Time (s)

³ Robert J. Kee, Michael E. Coltrin and Peter Glarborg ,"Chemically Reacting Flow: Theory and Practice", 2003 – chap 16
 ⁴ http://cantera.github.io/docs/sphinx/html/reactors.html

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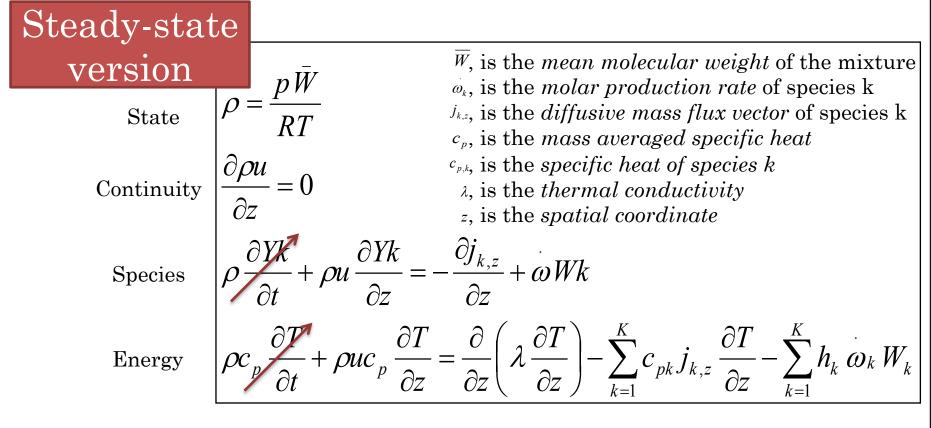
Computed solution to an atmospheric-pressure, freely propagating, stoichiometric, premixed, hydrogen-air, flat flame.

Picture from Robert J. Kee, Michael E. Coltrin and Peter Glarborg ,"Chemically Reacting Flow: Theory and Practice", 2003 – chap 3 Cantera related page : <u>https://cantera.org/science/flames.html</u>

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Governing equations Laminar Premixed Flame

For a steady laminar premixed flame, we consider 3+K equations, derived from the general conservation equations for perfect gas in cylindrical coordinates³:



³ Robert J. Kee, Michael E. Coltrin and Peter Glarborg, "Chemically Reacting Flow: Theory and Practice", 2003 – chap 16





Numerical Resolution

The *steady state* version of the previous equations (1D flames) are discretized on a generally **non uniform mesh**, if needed.

$$\left[\frac{dT}{dx}\right]_{j} = \frac{T_{j} - T_{j-1}}{x_{j} - x_{j-1}}$$

Example with the windward difference in space

Let's introduce

- **the discretized solution vector y** (density, velocity, mole fractions and temperature at each space point)

- the equation vector **F** (the 3+K conservation equations).
- the discretized residual F(y) at each space point.



The computational problem consists of **finding the smallest residual F**, (at all space points j ...).

F(y)=0

with $y = (solution _vector _pt1,..., solution _vector _ptJ)$

A Damped modified Newton solver with internal time integration is used (but then, transient terms are needed)

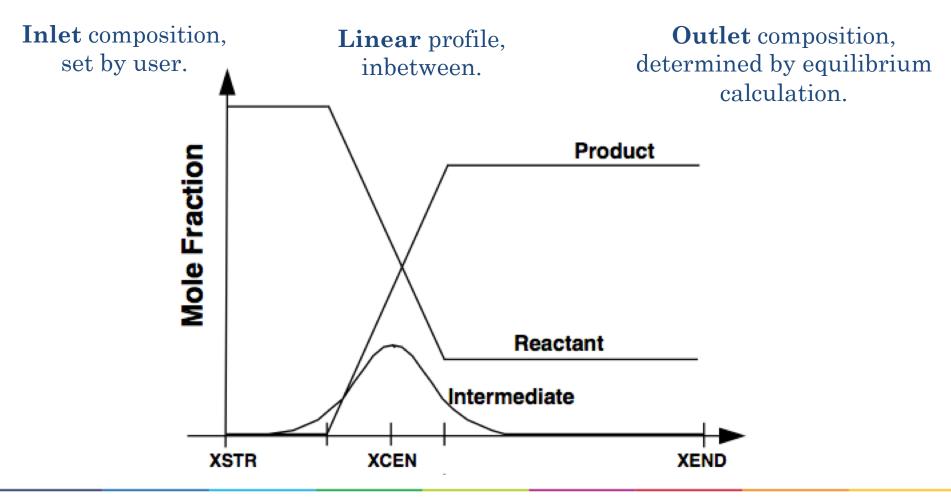
> Convergence relies on the **initial estimate**, y^0 , usually provided by equilibrium calculation at the inlet temperature T_1^0 and pressure P_1^0 .





Governing equations Numerical Resolution

An initial y^0 is required.



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Governing equations Numerical Resolution

A Damped modified Newton solver with internal time integration

The **Newton solver** is : the method used by Cantera to solve the system and try to find the solution.

It is **damped** because a damping coefficient is added to help for the convergence.

It is **with internal integration** as an "artificial temporal term" is added to help for the convergence if the damping failed.





Governing equations Numerical Resolution

The Newton solver

What we seek at point m is

$$F(y) = 0$$

which is used to iterate

$$\frac{\partial F}{\partial y} = \frac{0 - F(y^m)}{y^{m+1} - y^m}$$

or in other words

$$y^{m+1} = y^m - \left[\frac{\partial F}{\partial y}\right]_{y^m}^{-1} F(y^m)$$

- Convergence is reached when $\Delta y^m = y^{m+1} - y^m$ becomes negligibly small. - The mesh might be automatically refined in the region of high gradients

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The **Damped modified** Newton solver

Evaluating the Jacobian matrices

$$\left(\frac{\partial F}{\partial y}\right)_{y^m} = J^m$$

is a **time consuming process**, so it is not done at each iteration

The solver evaluates the Jacobian each specified number of iteration step and inbetween

$$(J^{m})^{-1} = \lambda^{m} \left(\frac{\partial F}{\partial y}\right)_{y^{k}}^{-1} = \lambda^{m} (J^{k})^{-1}; \quad 1 < k \le m \quad 0 < \lambda^{m} \le 1$$

so that the problem becomes

$$(J^k)\Delta y^m = -\lambda^m F(y^m)$$



The **Damped modified** Newton solver

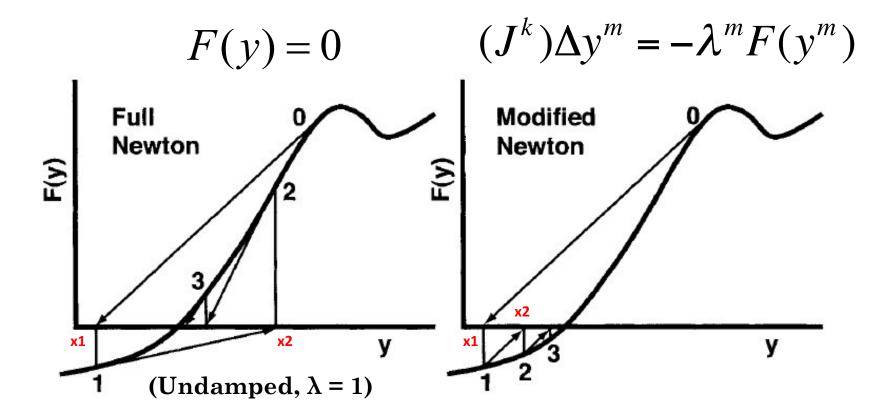


Illustration of the full Newton and modified Newton algorithm

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The **Damped modified** Newton solver

$$(J^k)\Delta y^m = -\lambda^m F(y^m)$$

The λ^m must satisfy the condition that the subsequent undamped step be smaller.

$$\left| \Delta y^{m+1} \right| \leq \left| \Delta y^m \right|$$
$$\left| (J^m)^{-1} F(y^{m+1}) \right| \leq \left| (J^m)^{-1} F(y^m) \right|$$

If not verified

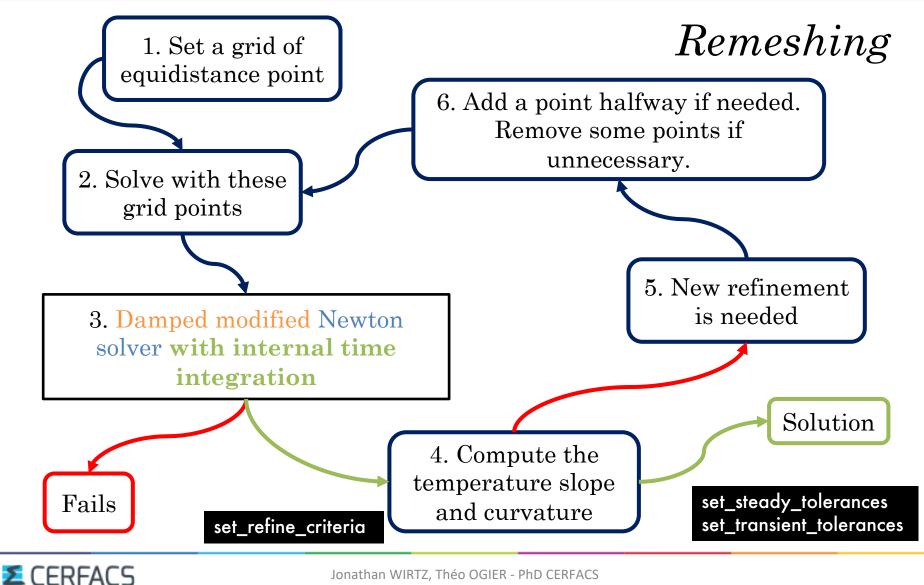
another damping parameter is tested a new Jacobian is computed <u>set_max_jac_age</u>



The Damped modified Newton solver with internal time integration

Whenever both damping parameters and the new Jacobian fail :

- **Transient equations** are used $F(y_{t=n+1}) = \frac{y_{t=n+1} y_{t=n}}{\Lambda t}$
- Time derivatives are approximated by first-order, implicit
 backwards finite differences schemes.
- Time steps are specified by the user $\Delta t = h$
- Same Newton method to solve the system of equations for each time step $G(y) = F(y) - \frac{dy}{dt} = 0 \quad \left(J - \frac{I}{h}\right)(y_{n+1} - y_n) = -G(y_n)$
- The new y is used as a new starting estimate for the steady state problem





Content of the presentation

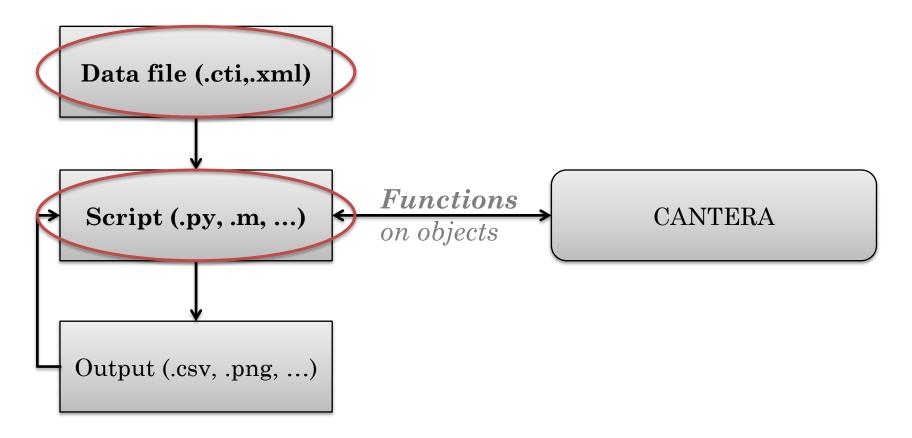
- I. Presentation of CANTERA
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Practical use

What do you need to run Cantera?





Practical use

• Where do you find the data file ?

- From CHEMKIN ('mech.inp', 'therm.dat' & 'trans.dat') via the tool ck2cti.
- From a dataset provided with CANTERA (air, GRIMech, ...).
- You can generate it by hand.
- And the script ?
 - You generate it from « building blocks ».



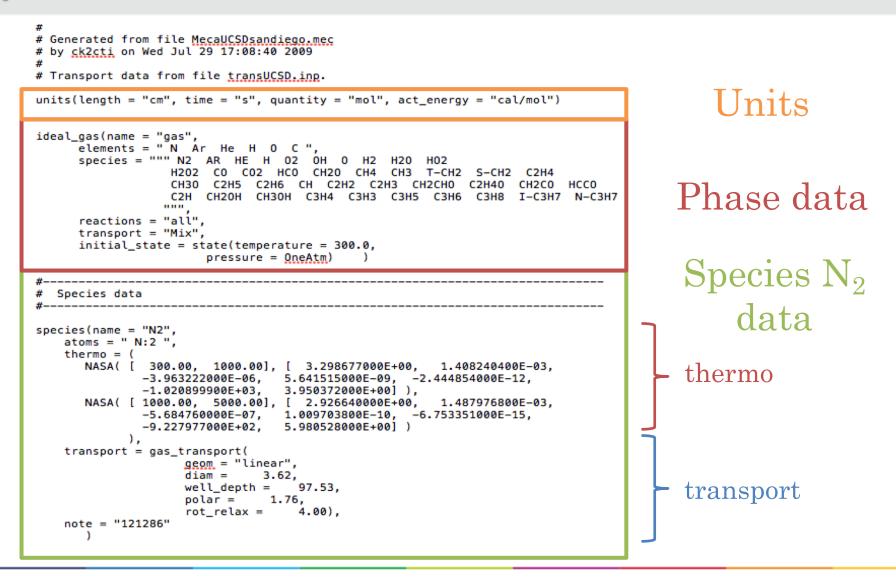


What is a data file (format '.cti') ?

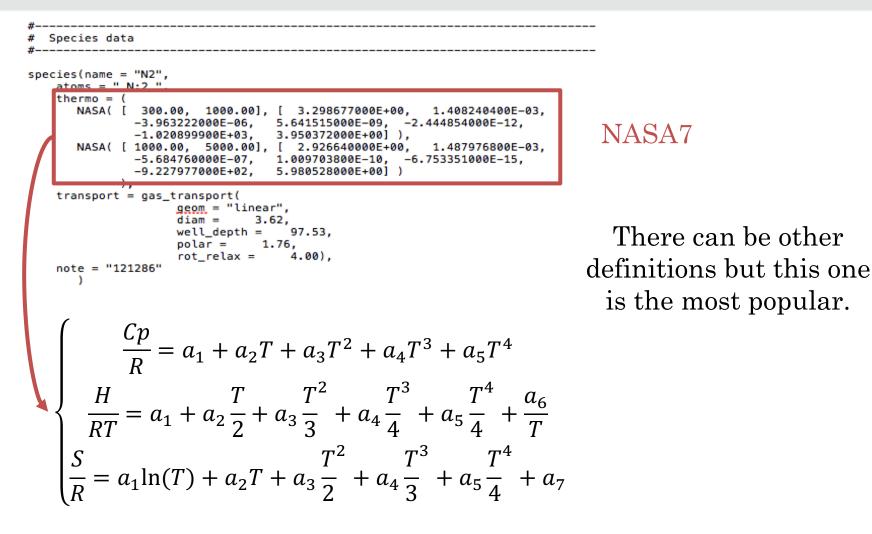
It contains information about :

- Phases and interfaces (species involved, thermo and transport models ...)
- Elements and species data
- **Reaction data** (expression, rate coefficients, pressure dependence, ...)
- <u>Appendix</u> gives you information about technical keywords





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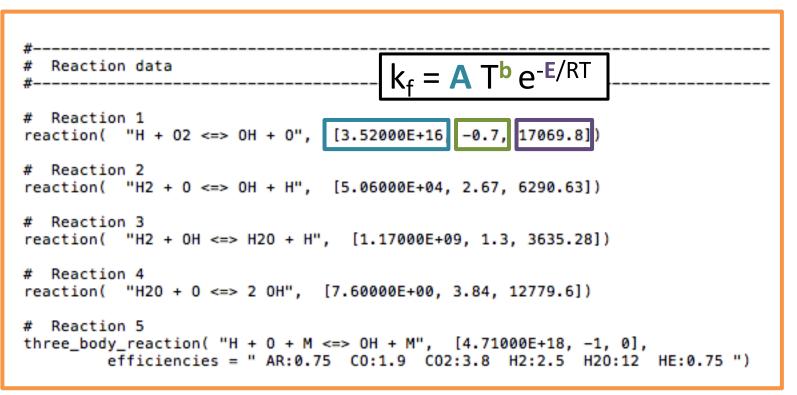


Cantera link : <u>https://cantera.org/science/science-species.html</u>



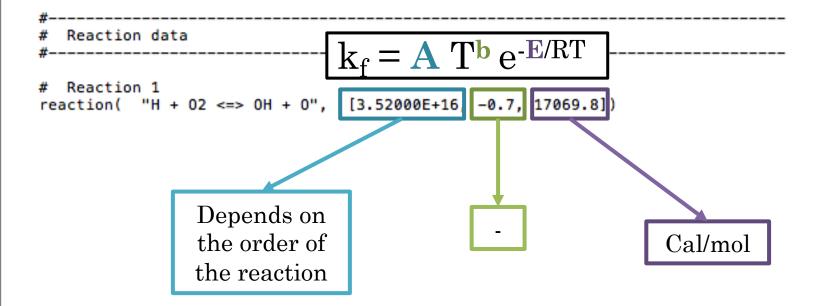


Reactions Data





units(length = "cm", time = "s", quantity = "mol", act_energy = "cal/mol")



Here : $\omega_{f,j} = k_f[O_2][H]$ So the order is 2 and the unit is : $[mol/m^3/s]/[mol/m^3]^2 = [mol^{-1}m^{-3}s^{-1}]$

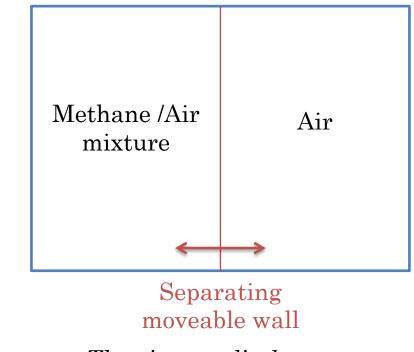
More data on the type of equations can be found in <u>appendix</u>.



Example **The constant pressure batch reactor**

It is composed of 5 main « building blocks »

- 2 Reactors
- Methane-air mixture
- Non reactive air mixture
- Moveable wall



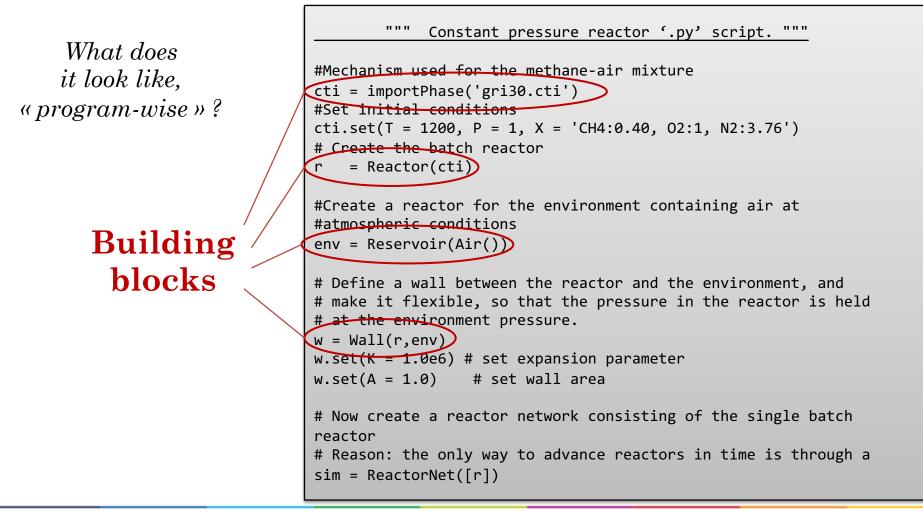
They form a constant pressure reactor !

The piston-cylinder system



Practical use Script

The constant pressure batch reactor



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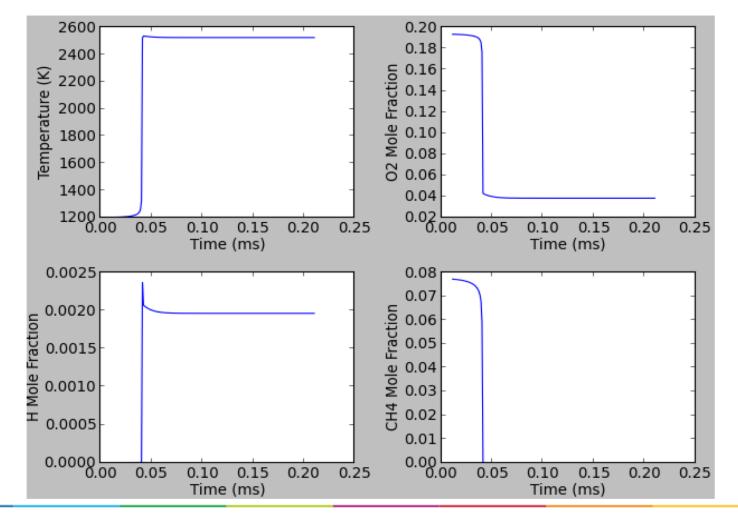


Practical use Script

The constant pressure batch reactor

What will you observe ?

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Practical use Helpful links

• Github https://github.com/Cantera/cantera

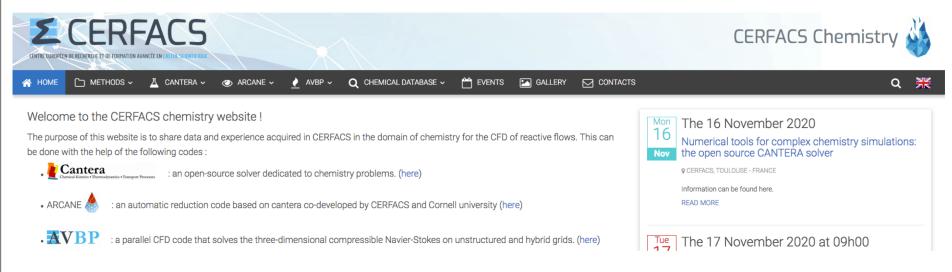
- Google Groups page for Cantera
 http://groups.google.com/group/cantera-users
- Cantera SourceForge Page <u>http://sourceforge.net/projects/cantera/files/</u>

To download all Cantera versions, source code or (Windows) binaries and find more documentation.



Practical use Helpful links

CERFACS CANTERA website : <u>https://chemistry.cerfacs.fr</u>



CERFACS knowledge and experience in chemistry for CFD in one website !!!

- Chemical database : Detailed, reduced and global kinetics mechanisms
- Cantera : CERFACS' version with installation walkthrough, scripts and tutorials
- *Private documentation* : ARCANE, AVBP
- *Events* : such as this training
- **CFD gallery** : nice pictures with great chemistry

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Official versions

You can install CANTERA on both LINUX, Windows and Mac.

To install the official version, instructions can be found here <u>https://cantera.org/install/index.html</u>

The current version is Cantera 2.4.0.







CERFACS versions

If you are from CERFACS get the sources with

git clone git@nitrox.cerfacs.fr:cantera/cantera-avbp.git

From outside, you can get them from : <u>https://chemistry.cerfacs.fr/en/cantera-installation/</u>





Installing CANTERA

The advised procedure for a local installation of the CERFACS Cantera version is

~/Codes\$ cd cantera-avbp/
~/Codes/cantera-avbp\$ python install_cantera.py

The script is only valid for NFS machines installation and Mac OSX installation.





Thank you for your attention ! Any questions ? Yes, please ask ! No, it's fine ! Tutorial time !!



Appendix

- 1. Cantera VS CHEMKIN
- 2. Detailed structure of Cantera
- 3. Gibbs function
- 4. Keywords in the cti format
- 5. Equations in the cti









◆ Its possibilities are **comparable to the CHEMKIN-II suite :**

CHEMKIN = a set of FORTRAN libraries	CANTERA = a set of C++ libraries
3 input files (thermo / transport / mechanism)	1 « data file » (everything)
« Interpreter step » to generate the binary input file	
A driver to stir the program towards simulations (<i>Keywords</i>)	A script to arrange « building blocks » into a simulation (<i>Interface objects</i> <u>and functions</u>)
Outputs written by the libraries	Outputs generated by the language of the script (Python, C++, Matlab, FORTRAN)





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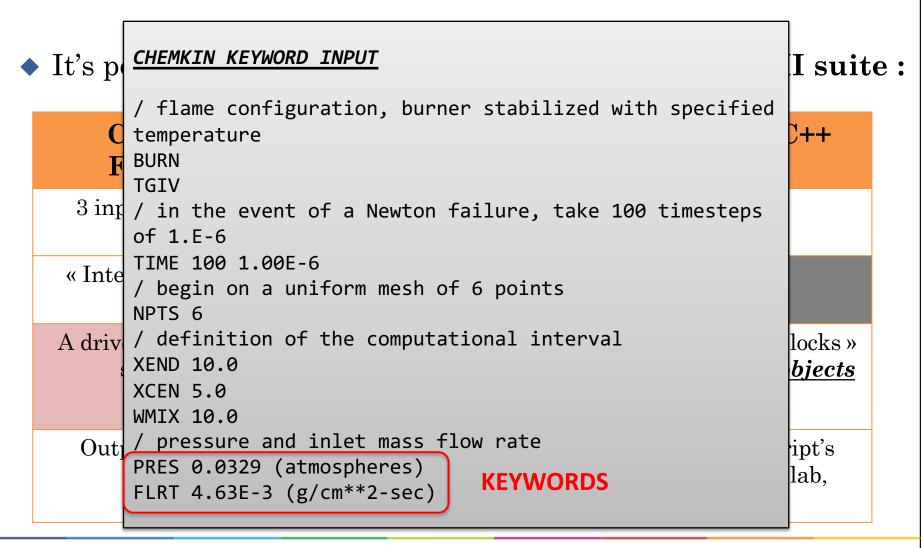




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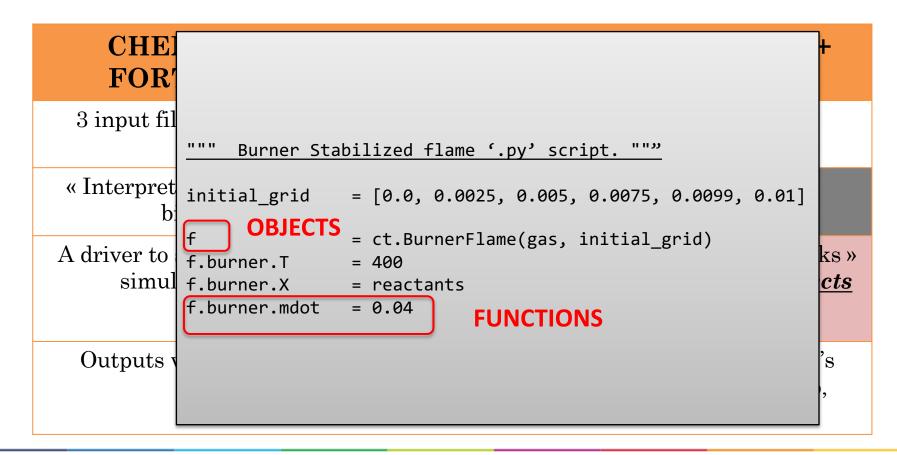
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◆ It's possibilities are **comparable to the CHEMKIN-II suite :**



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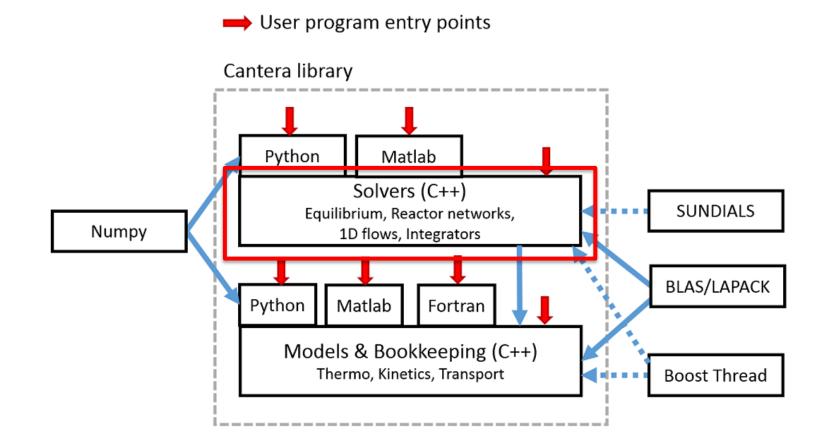


2. Detailed structure of Cantera





Structure of CANTERA







The « Solver » layer

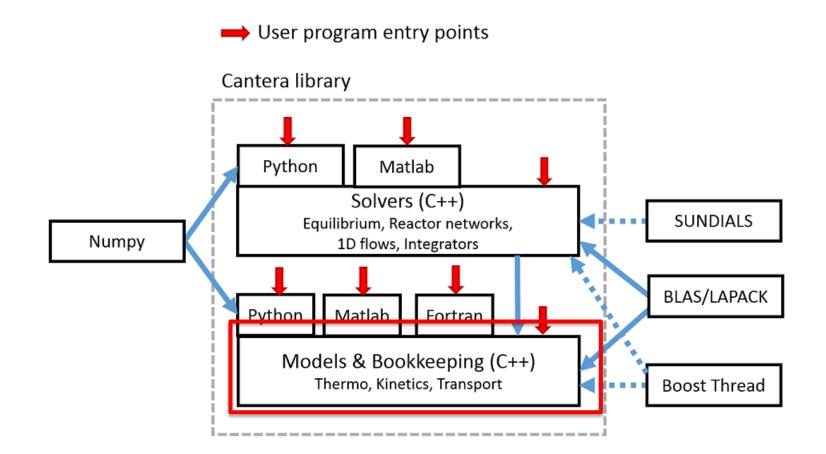
Usually hidden from the user, and **borrows from famous « free » libraries** (LAPACK, BLAS, ...) to perform

Equilibrium calculations
Reactor equations integration
1D calculations
...





Structure of CANTERA







The « Bookkeeping » layer

As we have just seen, it is the python script entry. **This layer contains all the methods that will**

• Initialize objects defined in the script

- If a phase object is defined, it will *calculate and set its thermodynamic state* and implement *their transport models* (example 1).
- Set the *inlet conditions* of a "FreeFlame" object (example 2).

◆ Link all objects together

• *Link two reactors* through a wall (example).

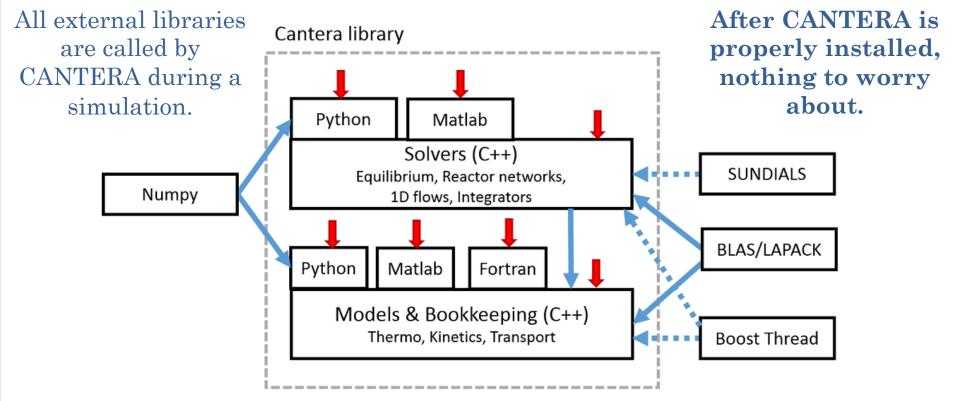
Organize the simulation

- Call the required solvers (so, the "solvers" layer)
- Extract required output data



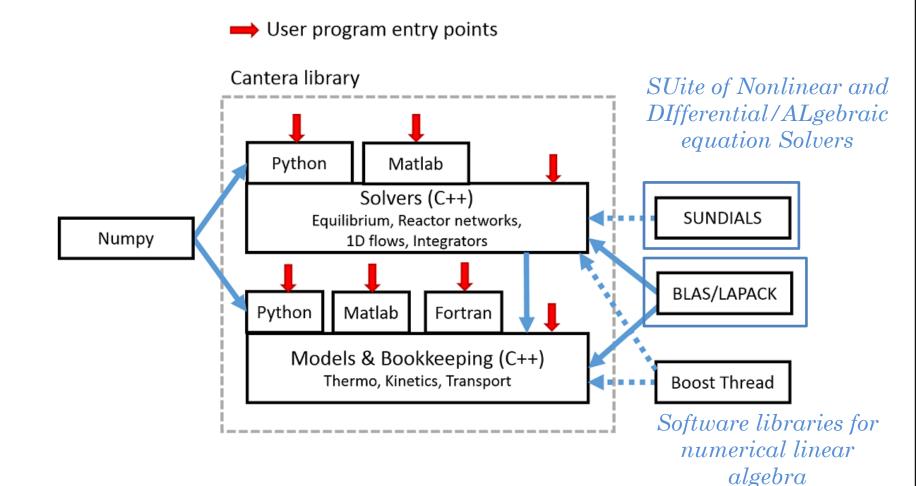
Cantera is a big lasagna, it has layers.





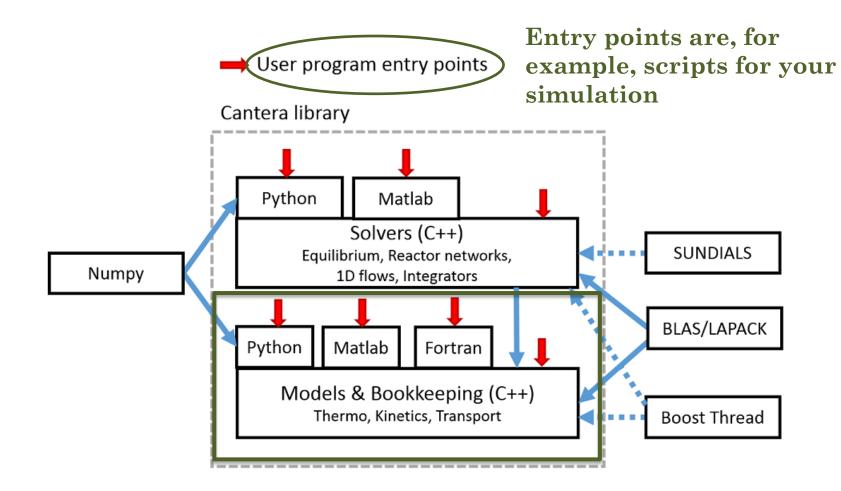
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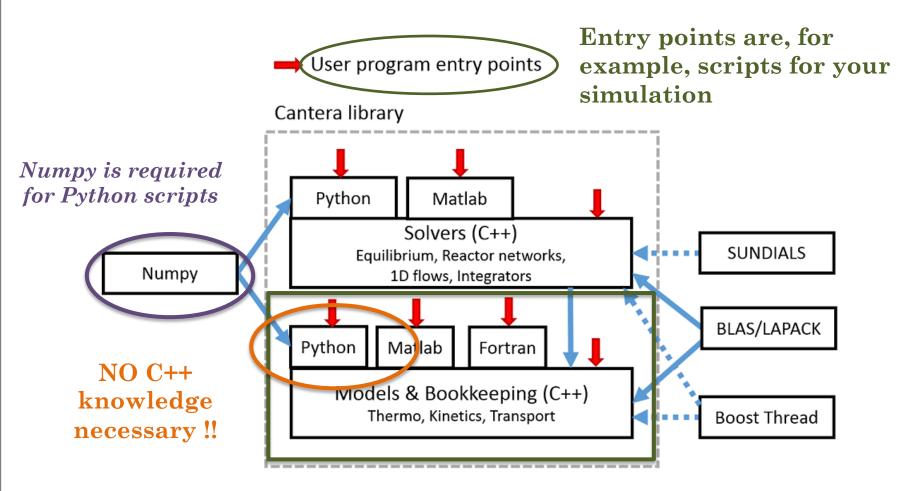
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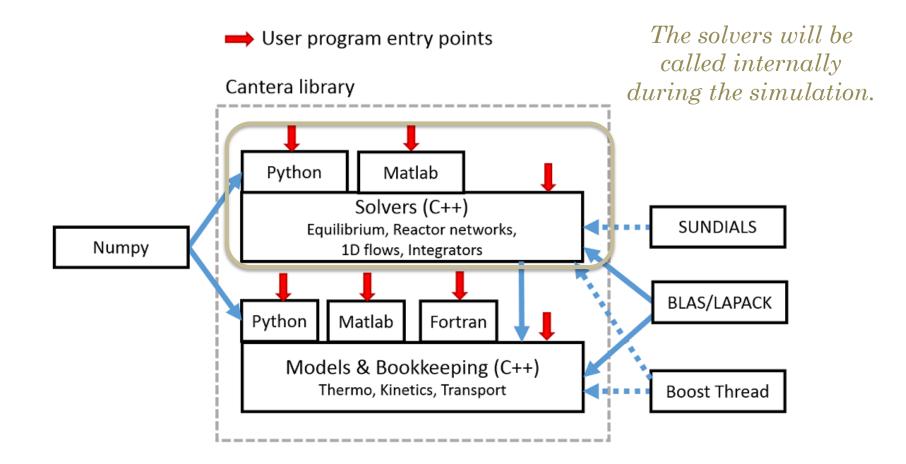
















3. Gibbs function





Example with the Gibbs function

"The equilibrium state is that corresponding to a minimum of a property called the energy function under specified conditions"

Use the Gibbs energy function G: $G = G(T, P, N_k)$

So that, when **P** and **T** are constant:

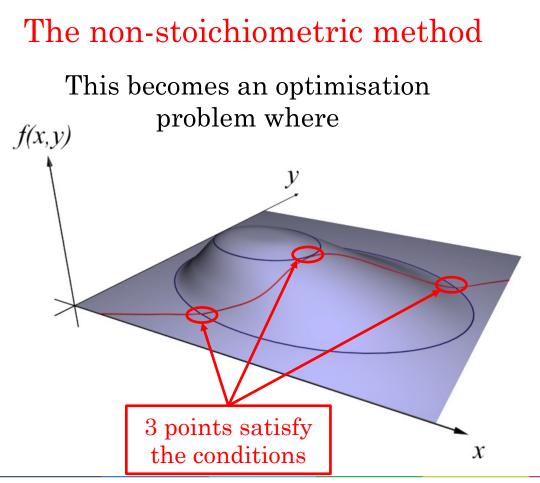
At equilibrium, we want to minimize G $dG = \sum_{k=1}^{K} \mu_k dN_k \quad \text{with} \quad \mu k = \frac{\partial U}{\partial Nk}$ $p_l = \sum_{k=1}^{K} n_{kl} N_k$

With the constraint that the number of moles \mathcal{P}_l of every element l (N, O, H, ...) is conserved:

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Example with the Gibbs function



$$dG = \sum_{k=1}^{K} \mu_k dN_k = 0$$
$$p_l^* = p_l - \sum_{k=1}^{K} n_{kl} N_k = 0$$

<u>Illustration in 2D</u>

- Find an extremum of the function G(x,y), represented by the blue lines

- that satisfies the condition
pl*(x,y)=smthg represented by
the red line

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Example with the Gibbs function

The non-stoichiometric method

This becomes an optimisation problem where

$$dG = \sum_{k=1}^{K} \mu_k dN_k = 0$$
$$p_l^* = p_l - \sum_{k=1}^{K} n_{kl} N_k = 0$$

Which is solved by **introducing** Lagrange multipliers λ_l such that

And the problem can be posed as a solution of a set of (K + l) nonlinear equations

$$G^* = G + \sum_{l=1}^{L} \lambda_l p_l^*$$

$$\frac{\partial G^*}{\partial N_k} = \mu_k - \sum_{l=1}^L \lambda_l n_{kl} = 0$$
$$\frac{\partial G^*}{\partial \lambda_l} = p_l^* = 0$$

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The non-stoichiometric method

Once the λ_l are determined, since **T & P are constant**, the mole fractions are automatically deduced.

$$\mu_k = \sum_{l=1}^{L} \lambda_l n_{kl} \Longrightarrow X_k = \frac{P_o}{P} \exp(-\frac{g_k^0(T)}{RT} + \sum_{l=1}^{L} n_{kl} \frac{\lambda_l}{RT})$$

- General procedure (Note: no need to provide reactions information !) :
 The g⁰_k are tabulated.
- The user provides a guess for enough (L) X_k with the knowledge that $\sum_{k=1}^{n} X_k = 1$
- The λ_l can then be deduced from the previous K equations.
- The unkown X_k are calculated with those estimated λ_l and $\sum_{k=1}^{K} X_k$ is evaluated.
- If $\sum_{k=1}^{K} X_k$ is « too far » from 1, a new guess for the X_k is provided and the procedure reiterates with well chosen LX_k

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4. Keywords in the cti format





Practical use Data file

So... how is it written (format '.cti') ?

It is **composed of « entries » and « directives »** recognized via keywords.





Practical use Data file

So... how is it written (format '.cti') ?

It is **composed of « entries » and « directives »** recognized via keywords.

A directive will tell the code how the entry parameters are to be interpreted.

For example, the 'units' directive

units(length = "cm", time = "s", quantity = "mol", act_energy = "cal/mol")





Practical use Data file

So... how is it written (format '.cti') ?

It is **composed of « entries » and « directives »** recognized via keywords.

An entry defines an object.

For example, a falloff reaction

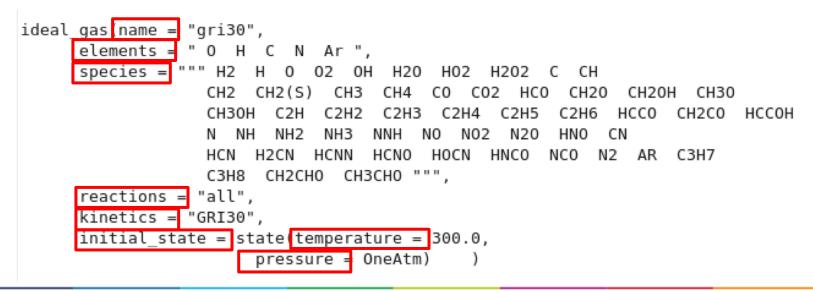


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Practical use Data file

So... how is it written (format '.cti') ? It is composed of « entries » and « directives » recognized via keywords. Entries are composed of a series of <u>fields</u> that can be assigned values.

For example, 'name' or 'elements' for a phase





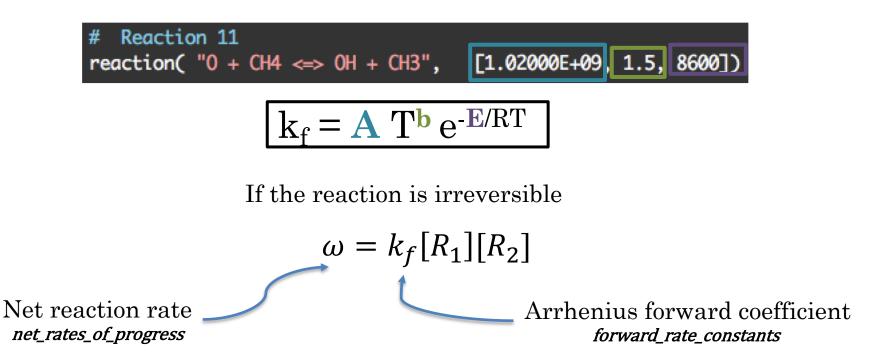
5. Equations in the cti





Practical use Data file

Simple forward constant rates coefficients



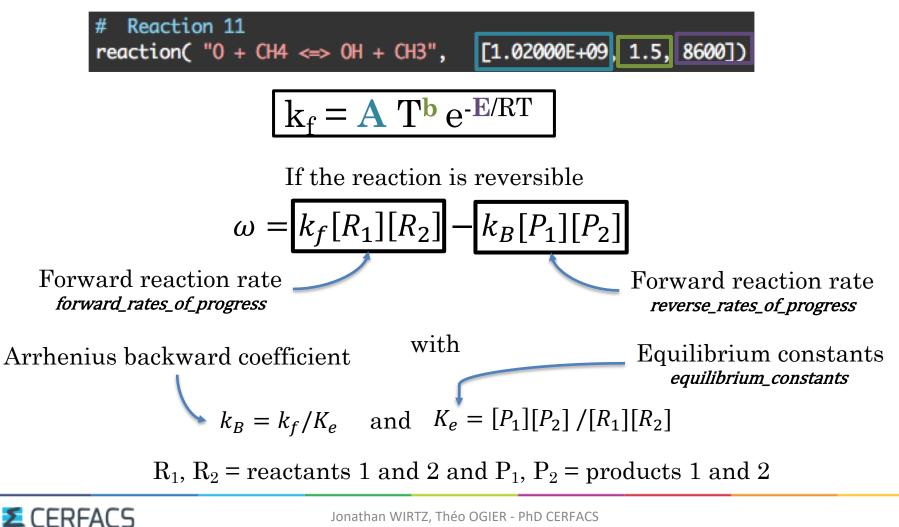
 R_1 , R_2 = reactants 1 and 2

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Practical use Data file

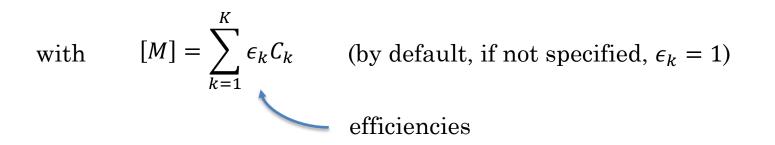
Simple forward constant rates coefficients



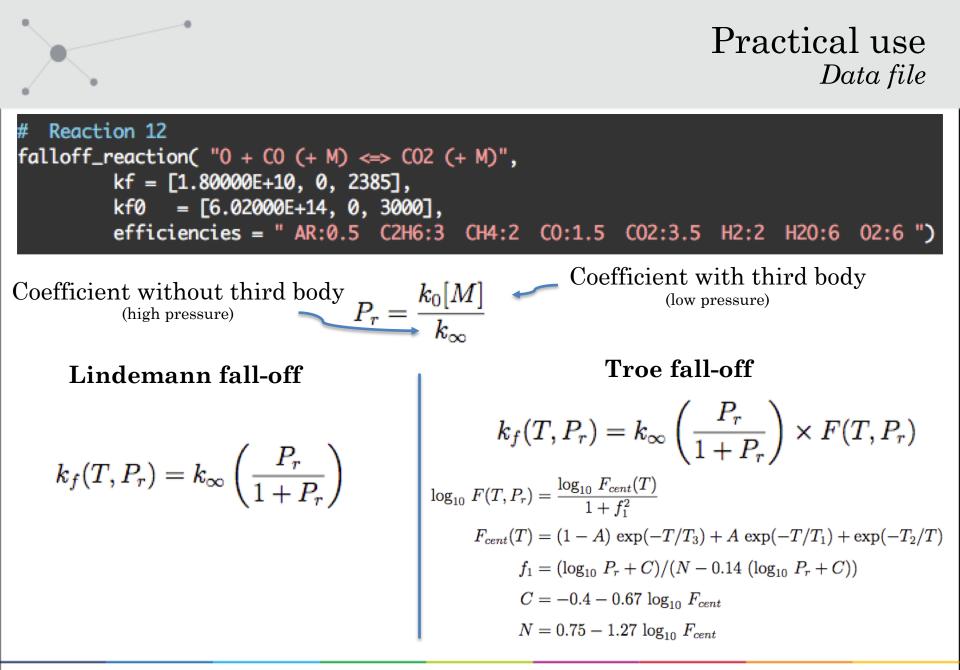


Practical use Data file

$$\omega = k_f[H][O_2][M] - k_B[HO_2][M]$$







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